14.63. Model: A completely inelastic collision between the bullet and the block resulting in simple harmonic motion. Visualize: $v_B = 0$



Solve: (a) The equation for conservation of energy after the collision is

$$\frac{1}{2}kA^2 = \frac{1}{2}(m_{\rm b} + m_{\rm B})v_{\rm f}^2 \Rightarrow v_{\rm f} = \sqrt{\frac{k}{m_{\rm b} + m_{\rm B}}}A = \sqrt{\frac{2500 \text{ N/m}}{1.010 \text{ kg}}}(0.10 \text{ m}) = 4.975 \text{ m/s}$$

The momentum conservation equation for the perfectly inelastic collision $p_{after} = p_{before}$ is

$$(m_{\rm b} + m_{\rm B})v_{\rm f} = m_{\rm b}v_{\rm b} + m_{\rm B}v_{\rm B}$$

(1.010 kg)(4.975 m/s) = (0.010 kg) $v_{\rm b}$ + (1.00 kg)(0 m/s) \Rightarrow $v_{\rm b}$ = 502 m/s

(**b**) No. The oscillation frequency $\sqrt{k/(m_{\rm b} + m_{\rm B})}$ depends on the masses but not on the speeds.